

# Benefit of tracking GNSS satellites with SLR

D. Thaller<sup>1)</sup>, R. Dach<sup>1)</sup>, G. Beutler<sup>1)</sup>,  
M. Mareyen<sup>2)</sup>, B. Richter<sup>2)</sup>

(1) *Astronomical Institute, University of Bern (AIUB), Switzerland*

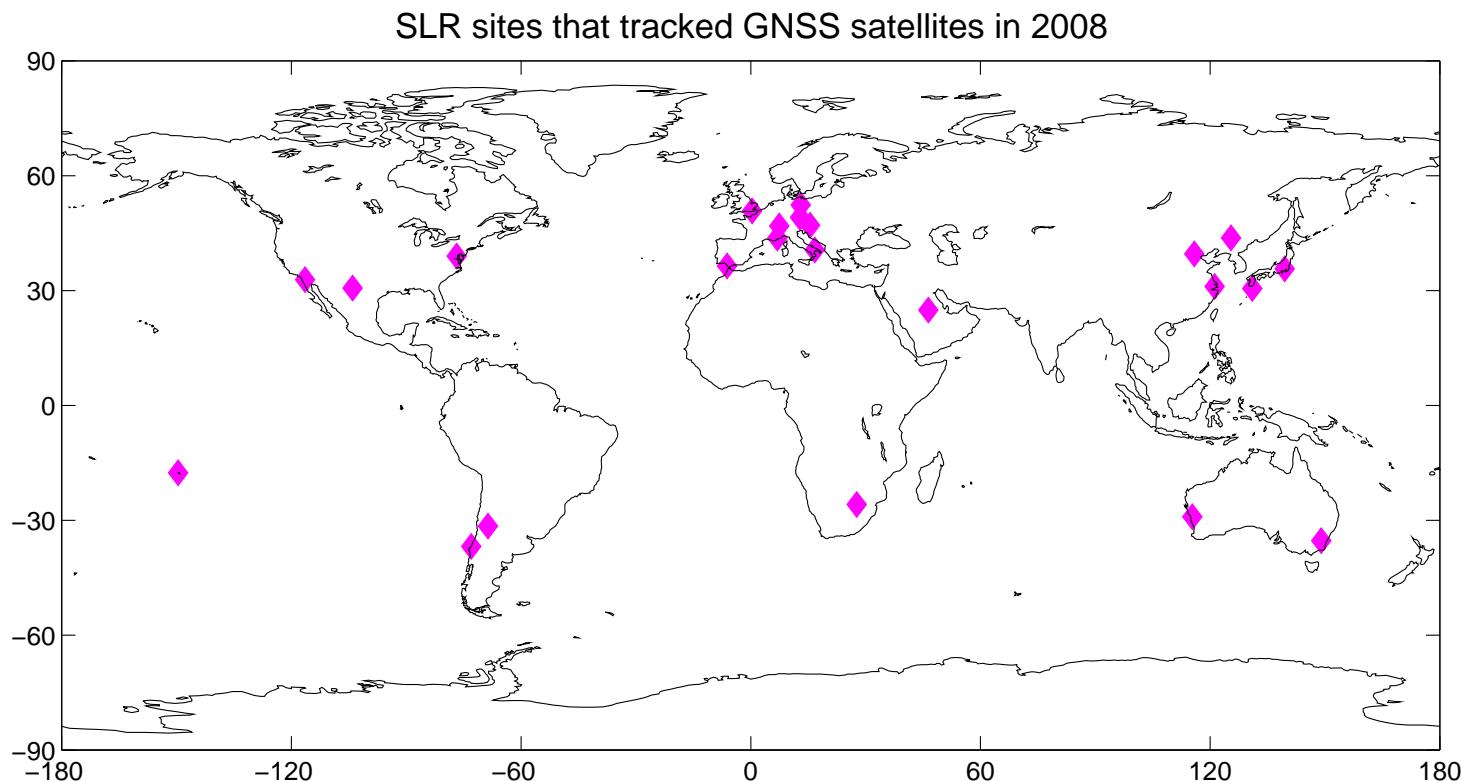
(2) *Bundesamt für Kartographie und Geodäsie (BKG), Frankfurt / Main, Germany*

# Overview

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1. **Statistics**
2. Two major applications:
  1. GNSS orbit validation using SLR
  2. **Combined GNSS+SLR solution**
3. **Expectation** from a combination GNSS and SLR@GNSS
4. **Results** from one year of combining GNSS and SLR@GNSS
5. Conclusions and outlook

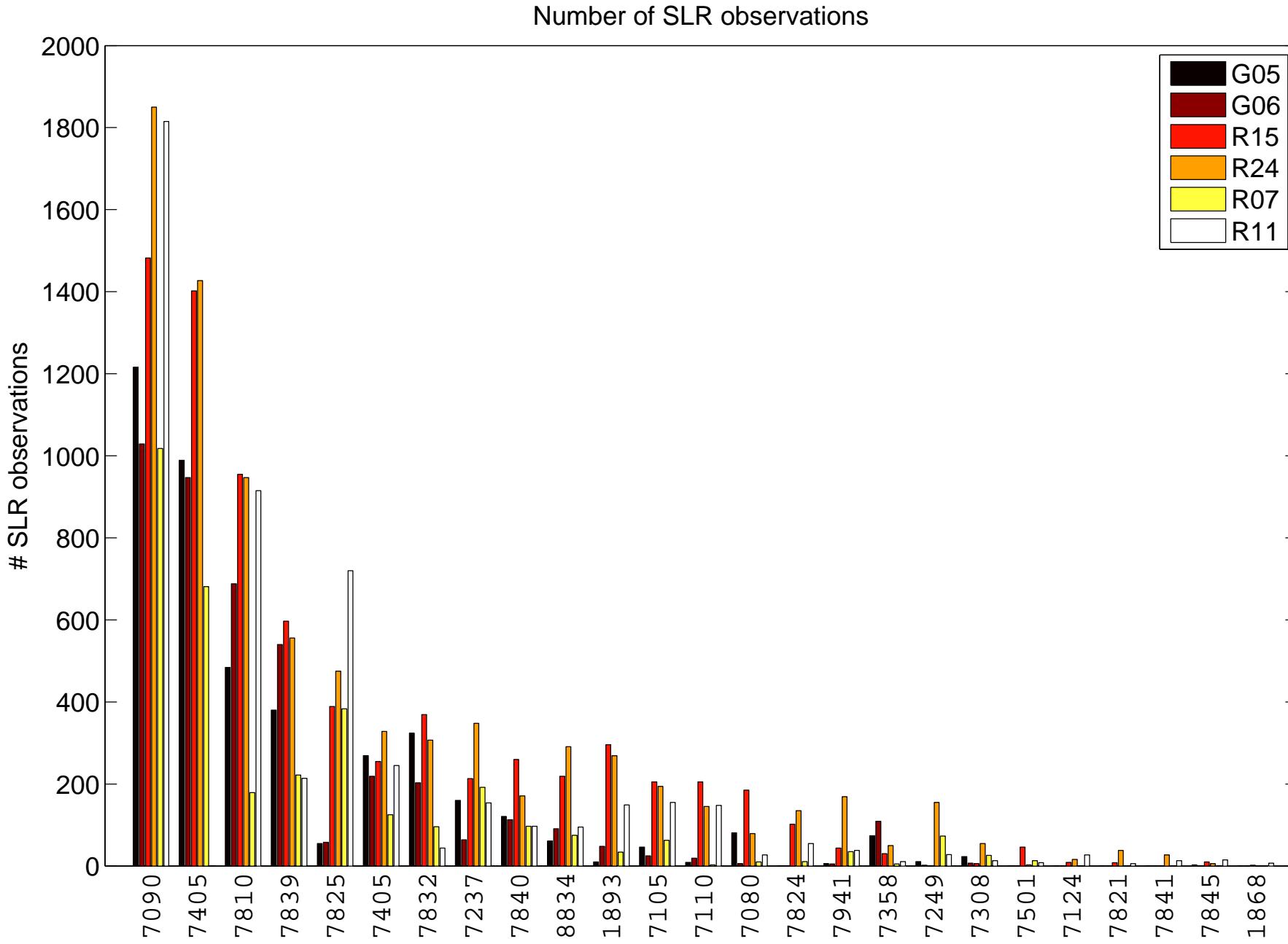
# Network in 2008



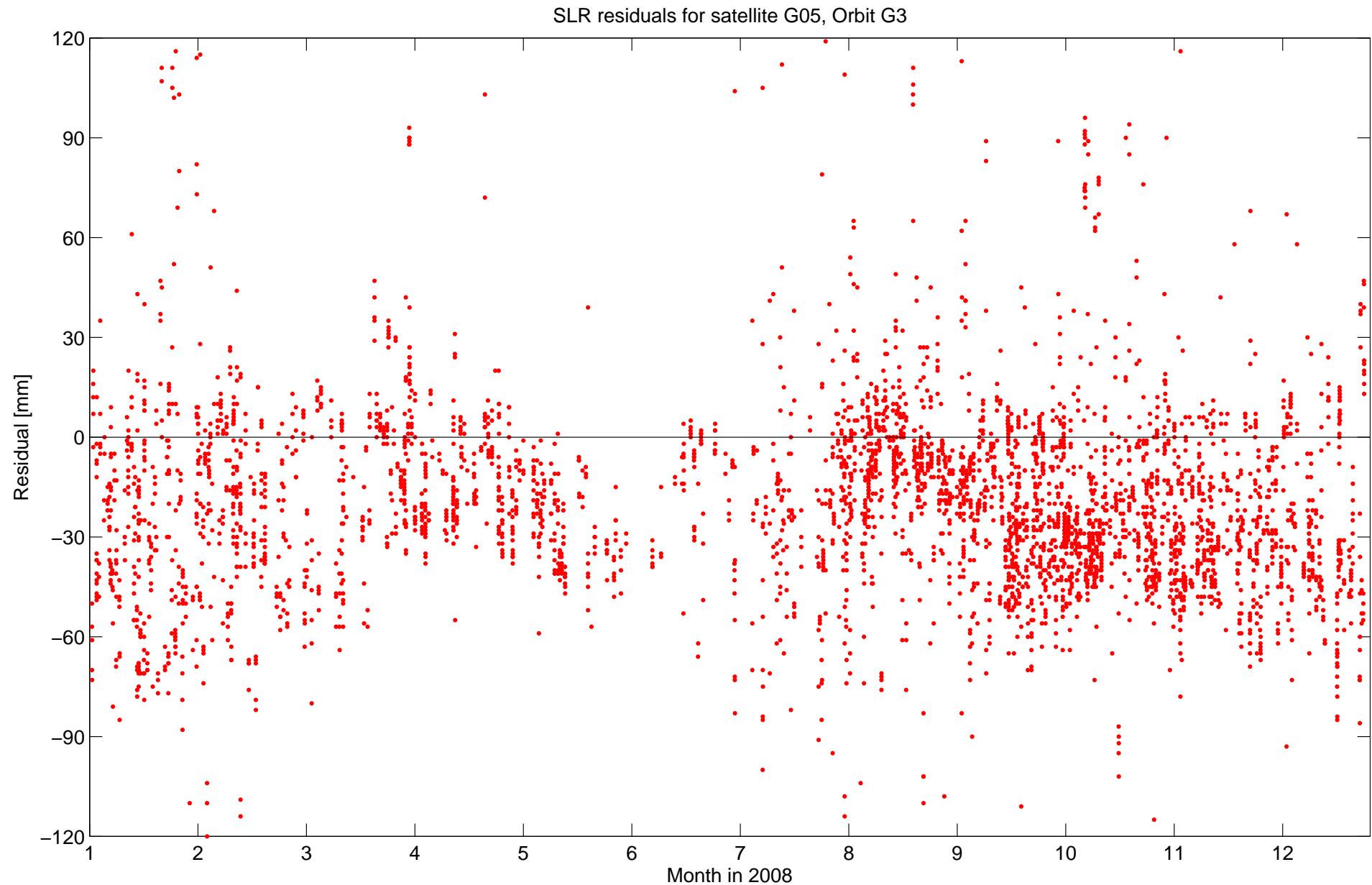
**Altogether:**  
25 SLR sites  
32165 normal points (NP)

8 sites with  $> 1000$  NP  
5 sites with  $> 500$  NP  
6 sites with  $> 100$  NP  
6 sites with  $< 100$  NP

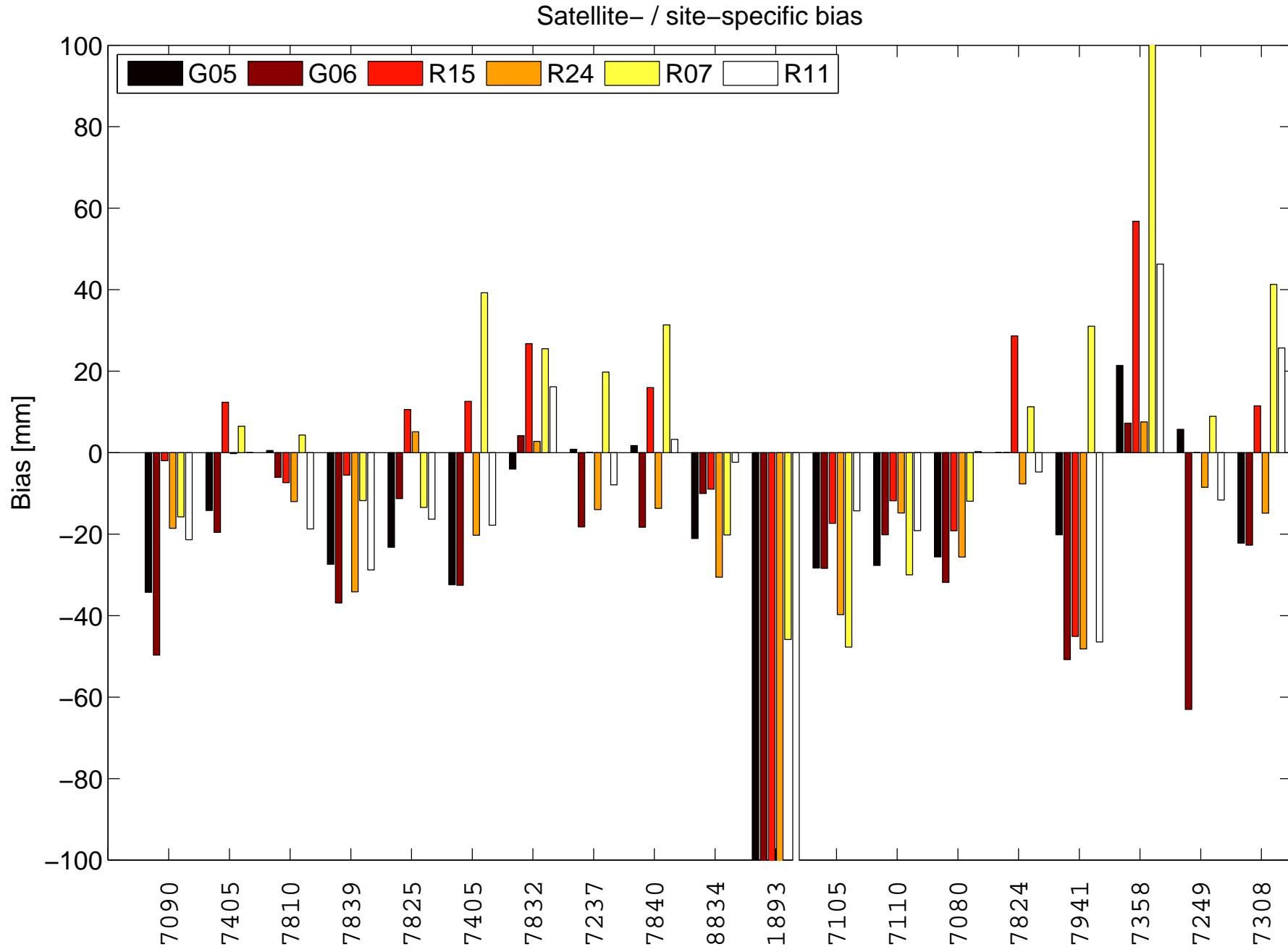
# Number of observations in 2008



# SLR residuals

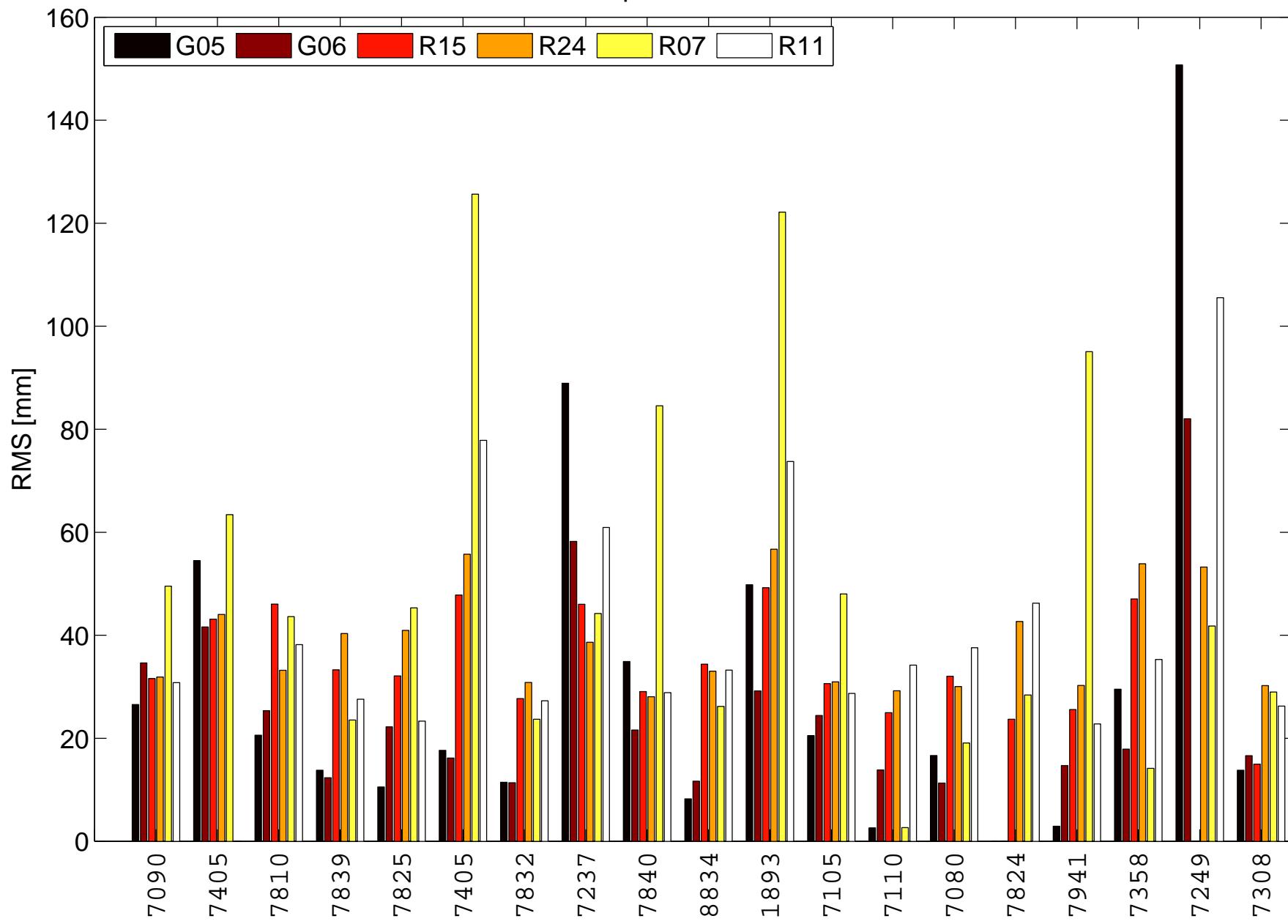


# SLR residuals: Mean Bias



# SLR residuals: RMS

Satellite- / site-specific RMS of SLR residuals



# Expectation from combined analysis

Strength of ***SLR to geodetic satellites*** (Lageos,...): Reference frame scale and geocenter  
⇒ **Applicable as well for SLR @ GNSS?**

***GNSS deficiencies***: modeling of radiation pressure and satellite antenna phase center

- Radiation pressure (RPR) correlated with **geocenter**
- Antenna phase center correlated with **scale**

⇒ GNSS scale and geocenter not “true”

## ***SLR@GNSS:***

- RPR parameters have to be estimated from SLR as well  
⇒ Geocenter is affected as well
- SLR observations independent from GNSS antenna phase center  
⇒ Scale can be gained from SLR

# Expectation from combined analysis

	GNSS @GNSS	SLR @GNSS	SLR @Lageos
<b>Radiation pressure ↔ Geocenter</b>	Problems in RPR modelling	Problems in RPR modelling	RPR well modelled
<b>GNSS satellite antenna phase center ↔ Scale</b>	Problems in phase center modelling	independent	-
<b>Range biases ↔ Scale</b>	-	To be defined	For a few sites only

## Other topics to be considered:

- “Local ties” and “space ties”

# GNSS+SLR combination

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- Studies using one year of data: 2008
- Analysis and combination with the *Bernese GPS Software*

→ ***GNSS-only NEQs (daily):***

- Combined GPS+Glonass analysis performed at CODE

→ ***SLR-only NEQs (daily):***

- SLR data to GPS and Glonass satellites
- Parameterization identical to GNSS analysis (orbits, ERP, geocenter)
- In addition: Range biases

→ ***Combination on normal equation level:***

- Daily combination
- Accumulation to annual solution
- Use of “space ties” only, no “local ties”!

# GNSS+SLR combination

## *Validation of estimated coordinates and of datum definition:*

- Comparison of coordinate differences at co-located GNSS–SLR sites using **local tie values**
- Helmert transformation of combined solution to GNSS-only and SLR-only solutions: **Scale**

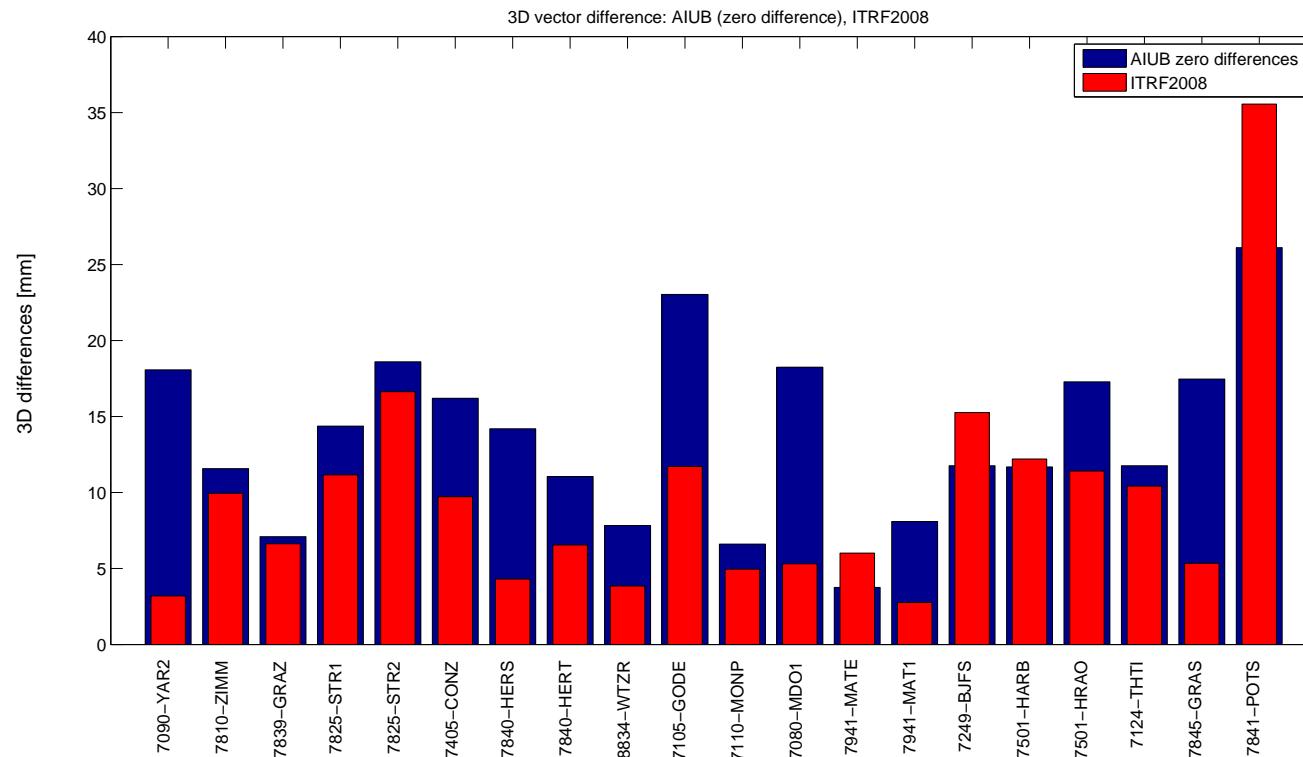
## *Parameters to be checked:*

- **SLR range biases**
- GNSS satellite antenna offsets
- Geocenter
- Orbits
- ...

# Comparison with local ties

## Level of agreement when using one year of data only

- Coordinate differences from GNSS-only and SLR-only solutions (1 year)
- Datum definition for both solutions using NNR+NNT (core sites)
- Velocities from ITRF2005



*Red:*  
ITRF2008 (prelim.)

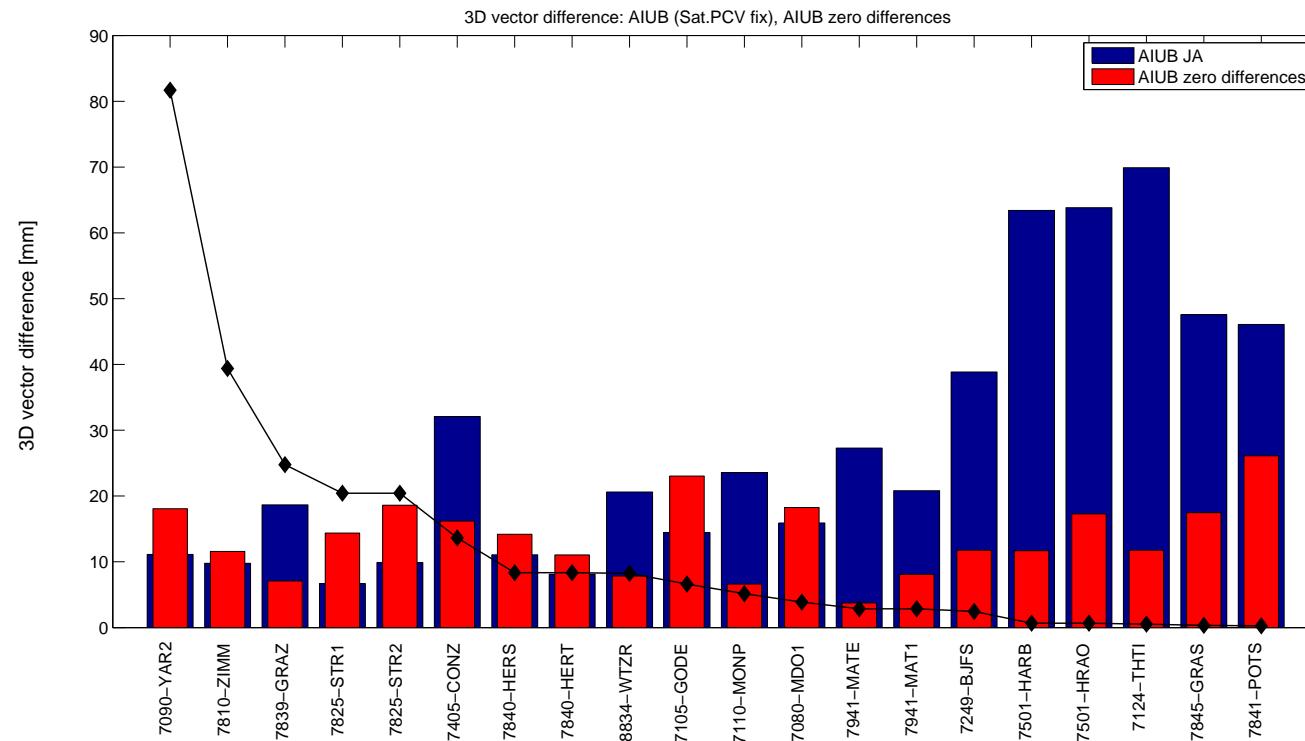
*Blue:*  
From annual  
single-technique  
solutions

*Plot provided by M. Seitz, DGFI*

# Comparison with local ties

**Changes when combining GNSS and SLR@GNSS using „space ties“ only**

- Combined yearly GNSS+SLR solution
- Datum definition: NNR+NNT (GNSS core sites), **no Local ties**
- **GNSS antenna phase center (SAO) fixed = Scale defined by GNSS and SLR**



**Red:**  
From annual  
single-technique  
solutions

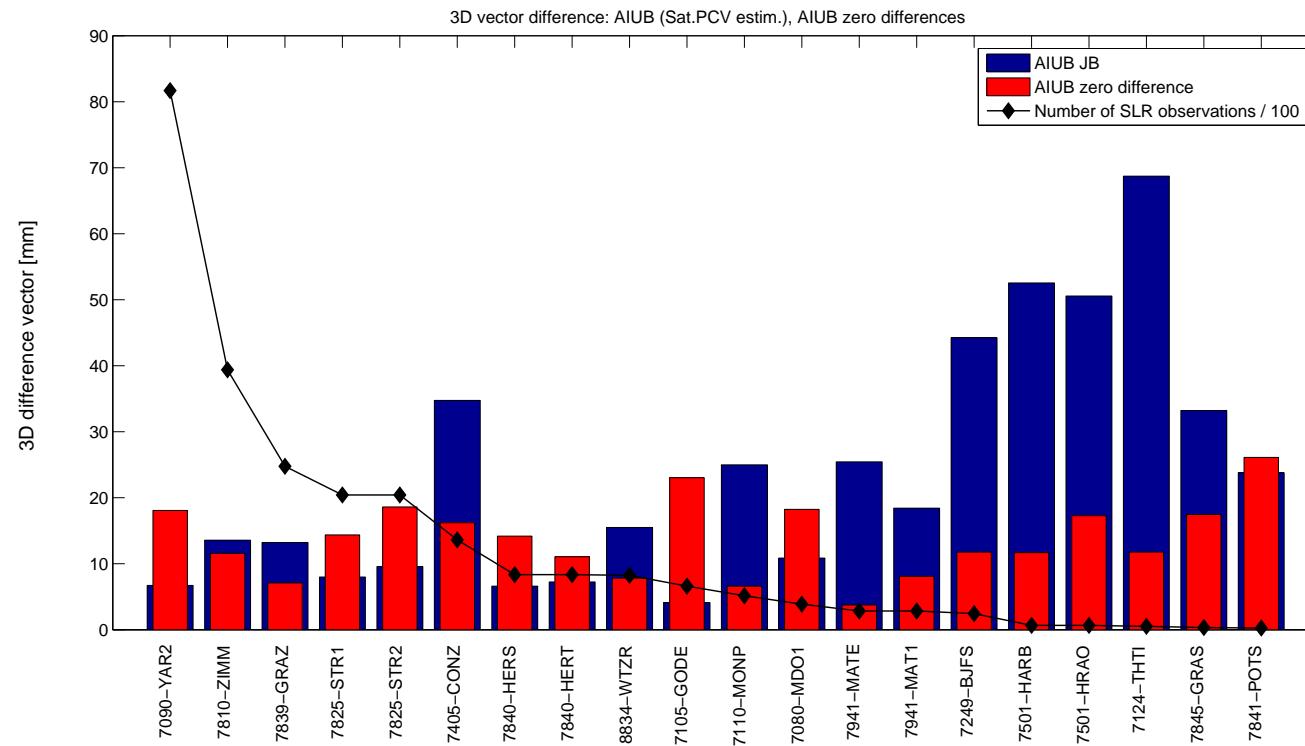
**Blue:**  
Combined solution,  
GNSS SAO fixed

*Plot provided by M. Seitz, DGFI*

# Comparison with local ties

Changes when combining GNSS and SLR@GNSS using „space ties“ only

- Combined yearly GNSS+SLR solution
- Datum definition: NNR+NNT (GNSS core sites), no Local ties
- **GNSS antenna phase center (SAO) estimated = Scale defined by SLR only!**



*Red:*  
From annual  
single-technique  
solutions

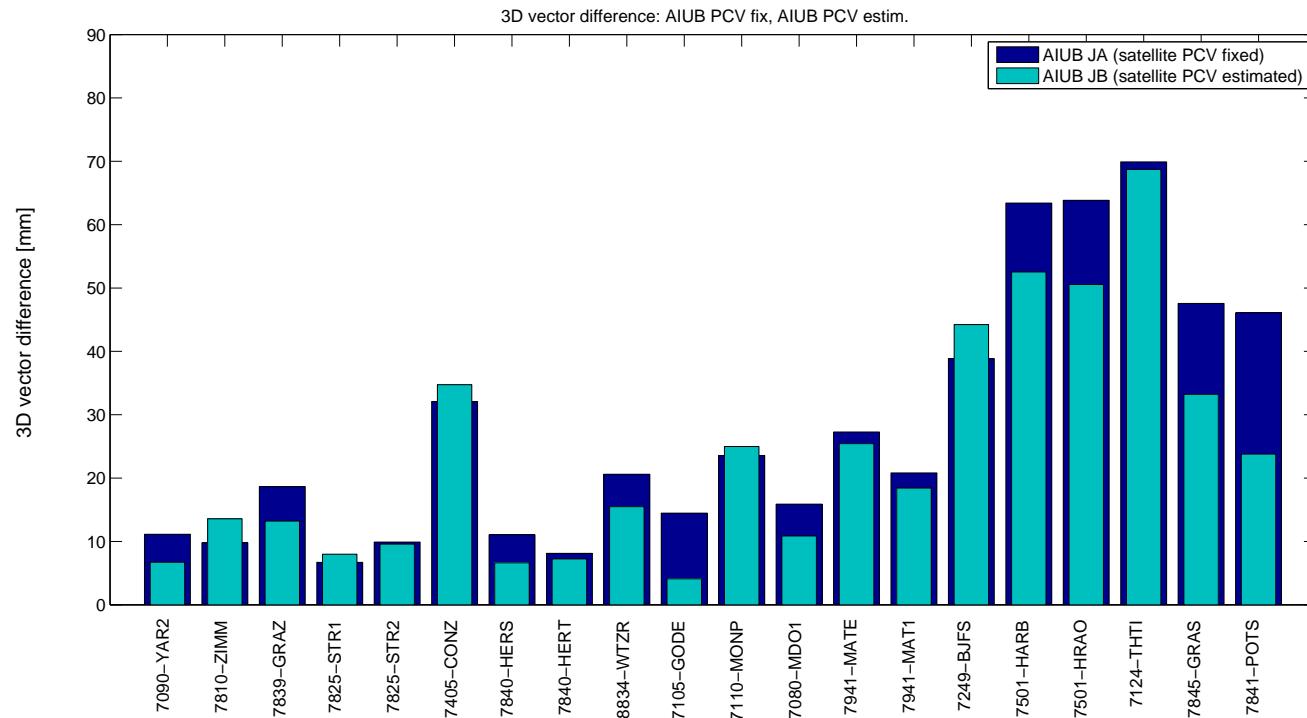
*Blue:*  
Combined solution,  
GNSS SAO estimated

Plot provided by M. Seitz, DGFI

# Comparison with local ties

## Impact of GNSS antenna phase center (SAO) estimation:

- No big differences ⇒ Estimation of SAO is possible
- Slightly better agreement with local ties if scale is NOT defined by GNSS (has to be verified using longer time span of data!)



*Blue:*  
Combined solution,  
GNSS SAO fixed

*Green:*  
Combined solution,  
GNSS SAO estimated

*Plot provided by M. Seitz, DGFI*

# SLR range biases

## Question 1:

*What is reasonable from technical point of view?*

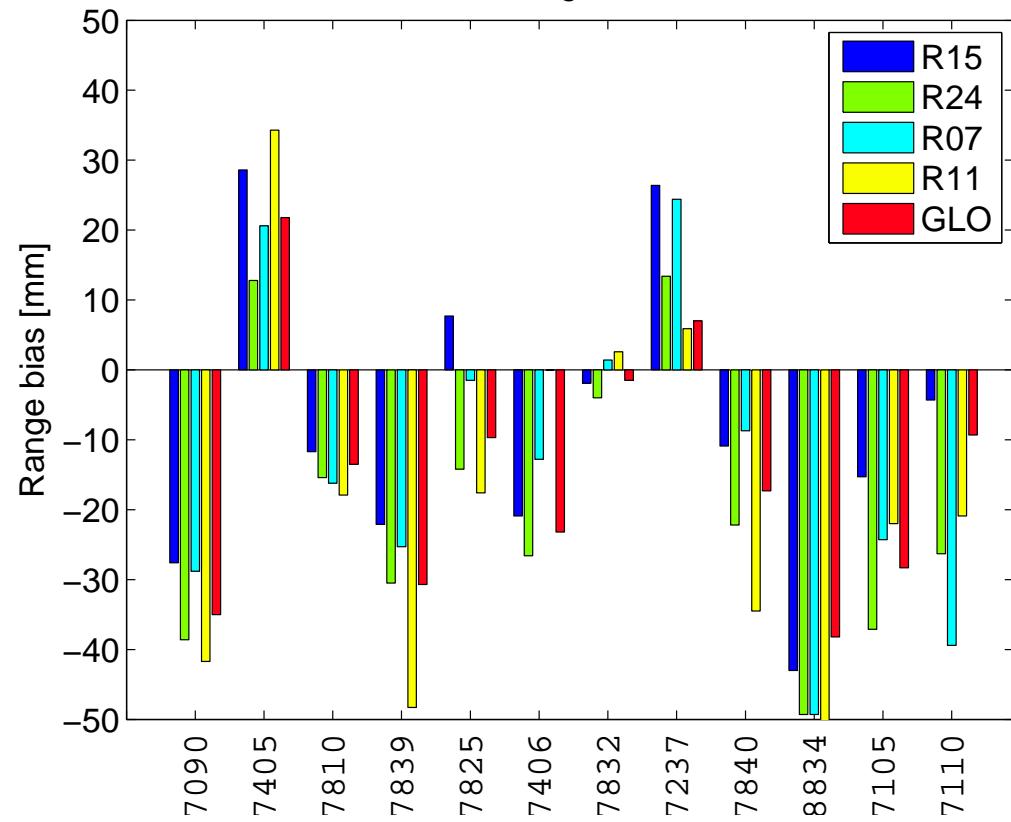
- Satellite-dependent? → Separate for every satellite
- System-dependent? → Average over GPS, over Glonass, ...
- Station-dependent? → Average over all GNSS satellites

## Question 2:

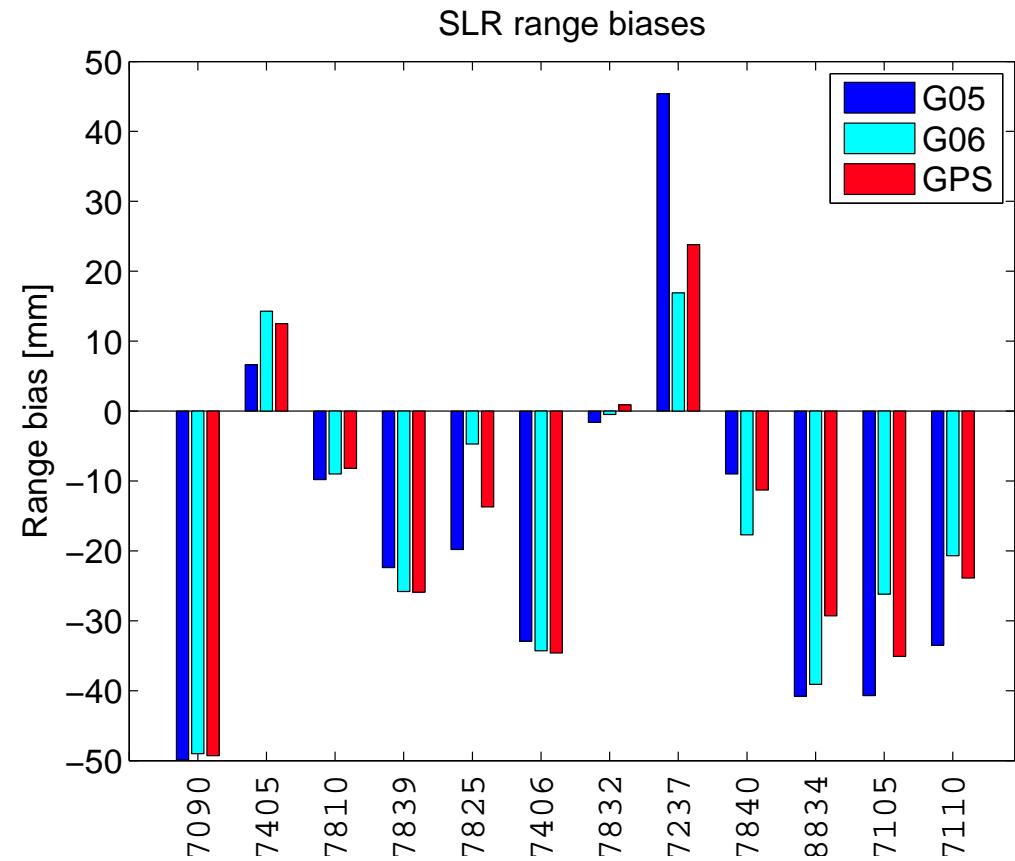
*Are the SLR range bias estimates influenced by estimating GNSS satellite antenna offsets?*

# SLR range biases

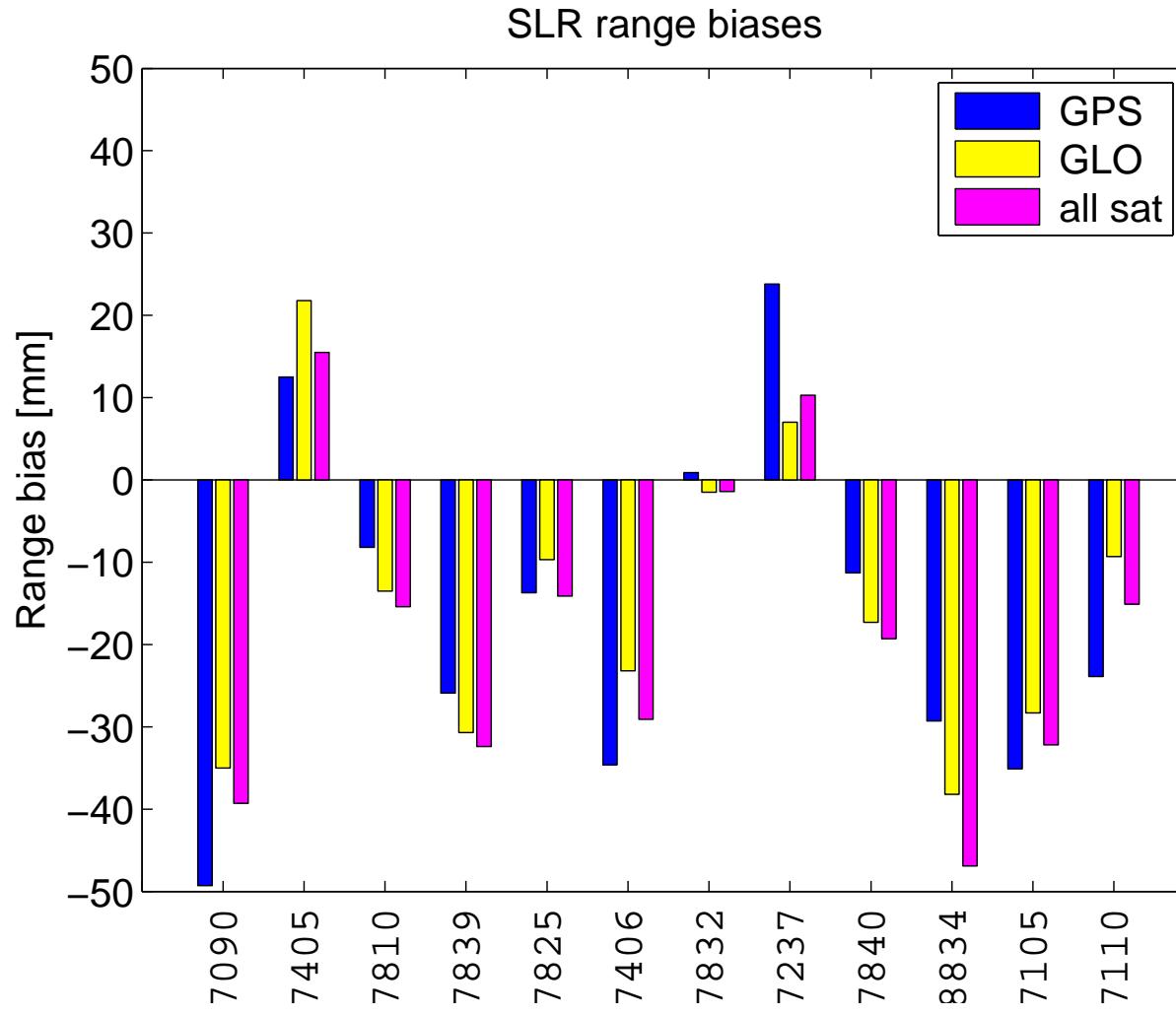
SLR range biases



System-specific range biases  
seem to be sufficient for most  
sites



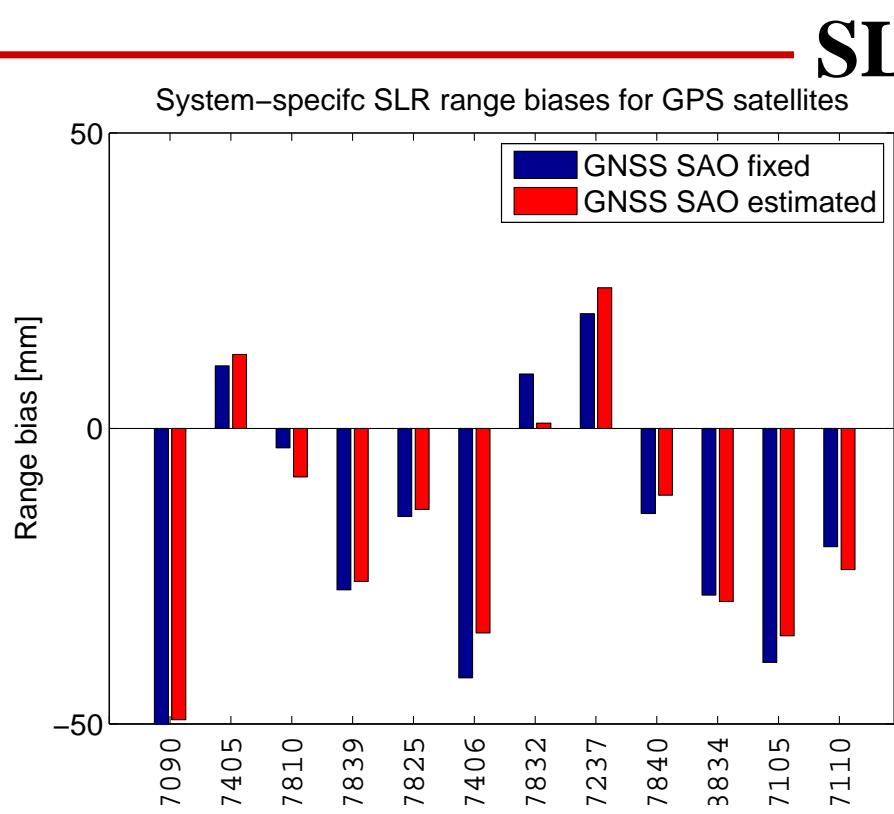
# SLR range biases



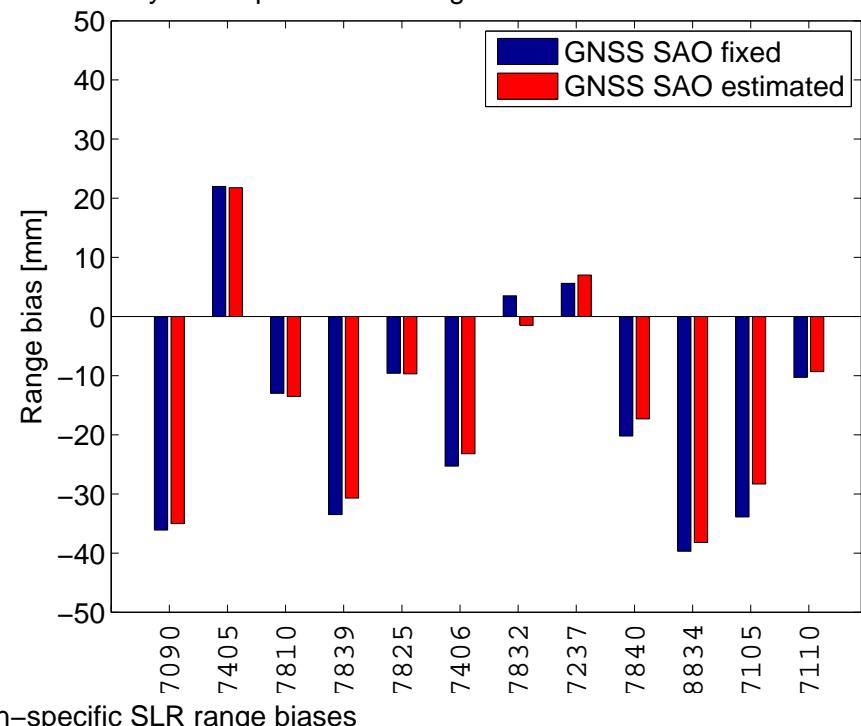
Station-specific range biases seem to be sufficient

# SLR range biases

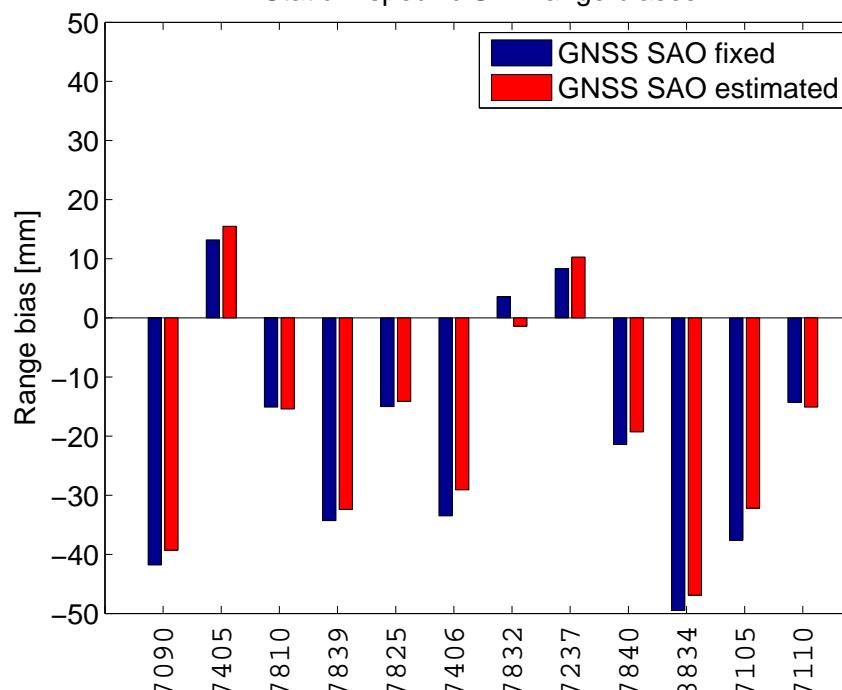
System-specific SLR range biases for GPS satellites



System-specific SLR range biases for Glonass satellites



Simultaneous estimation of  
GNSS antenna phase center  
offsets and SLR range biases  
is possible



# Scale between solutions (GNSS core sites)

$L$  = Satellite-specific SLR range biases

$K$  = System-specific SLR range biases

$J$  = Station-specific SLR range biases

	L1A	K1A	J1A		L1B	K1B	J1B	[ppb]
<b>GNSS-only</b>	0.0	0.0	0.0		<b>0.9</b>	<b>0.9</b>	<b>0.9</b>	
<b>L1A</b>		0.0	0.0		<b>0.9</b>	<b>0.9</b>	<b>0.9</b>	
<b>K1A</b>			0.0		<b>0.9</b>	<b>0.9</b>	<b>0.9</b>	
<b>J1A</b>					<b>0.9</b>	<b>0.9</b>	<b>0.9</b>	
<b>L1B</b>						0.0	0.0	
<b>K1B</b>								0.0
Lageos	$0.0 \pm 0.9$	$-0.8 \pm 0.7$	$-0.4 \pm 0.7$		$0.3 \pm 1.0$	$-0.6 \pm 0.6$	$-0.3 \pm 0.7$	

„A“: GNSS Sat.ant. fixed  
= Scale fixed

„B“: GNSS Sat.ant. estimated  
= Scale free  $\Rightarrow$  from SLR

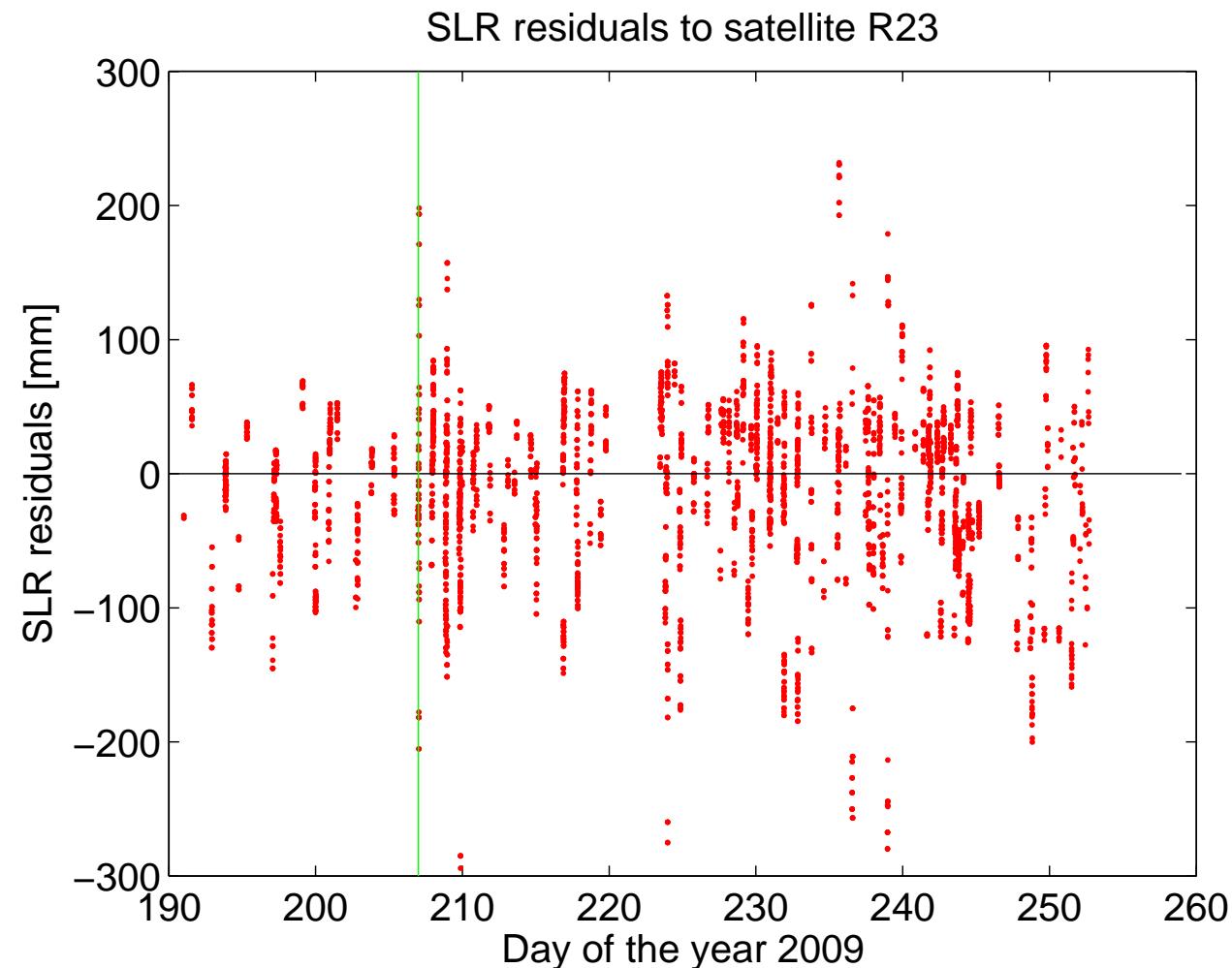
# Conclusions and outlook

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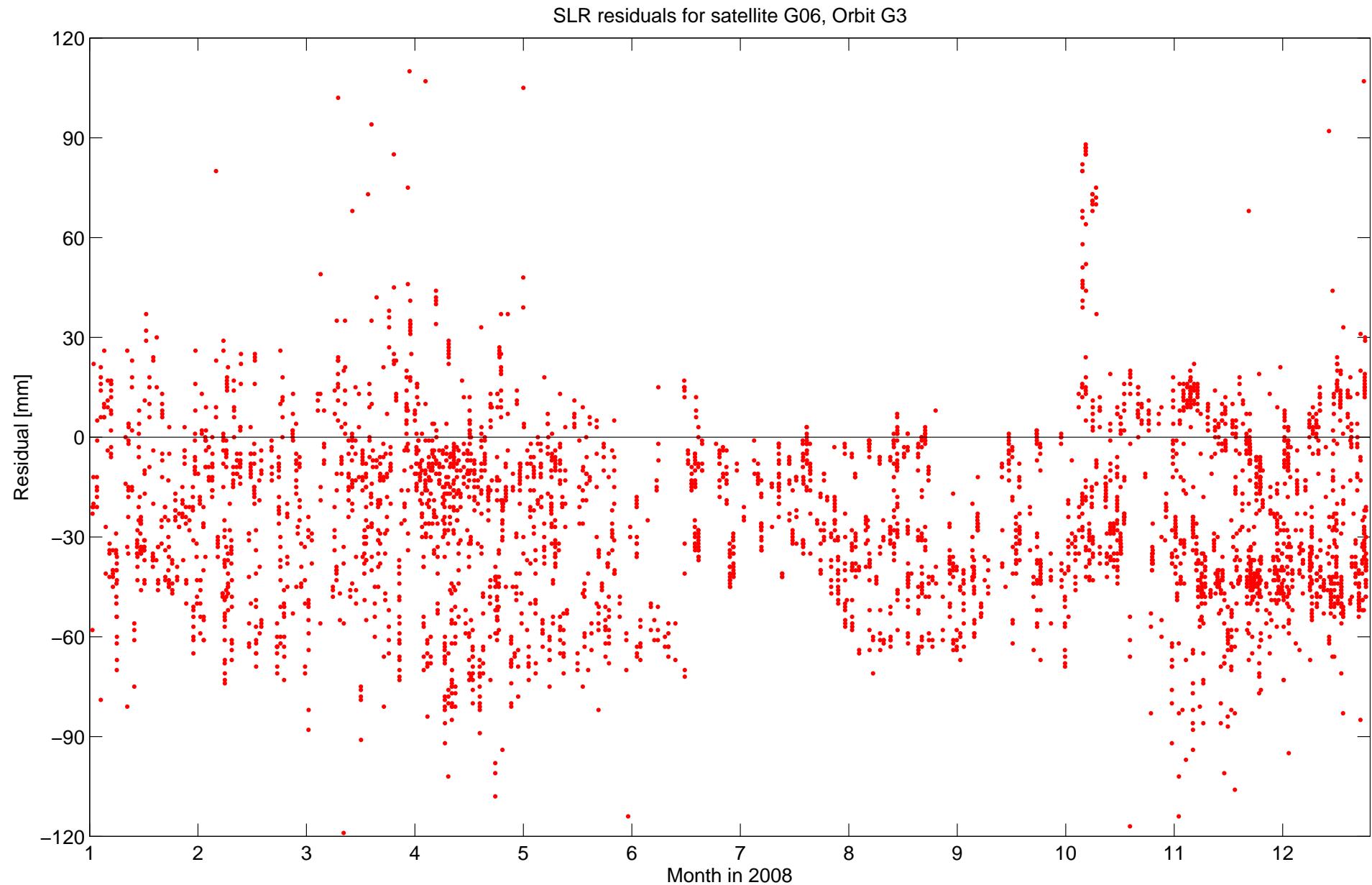
- Combination on *observation level* using SLR@GNSS works fine
- Connection via „*space ties*“ is possible (without local ties)  
*BUT:*  
*Accurate ties* (in space and on sites) required for combination
- *Scale from SLR* can be transferred to GNSS (estimation of GNSS SAO)
- Open question: Best *handling of SLR range biases* to GNSS satellites?
- Studies have to be extended to *longer time span*
- Thanks to Manuela Seitz from DGFI for providing comparisons with local tie values!

# SLR orbit validation for R23

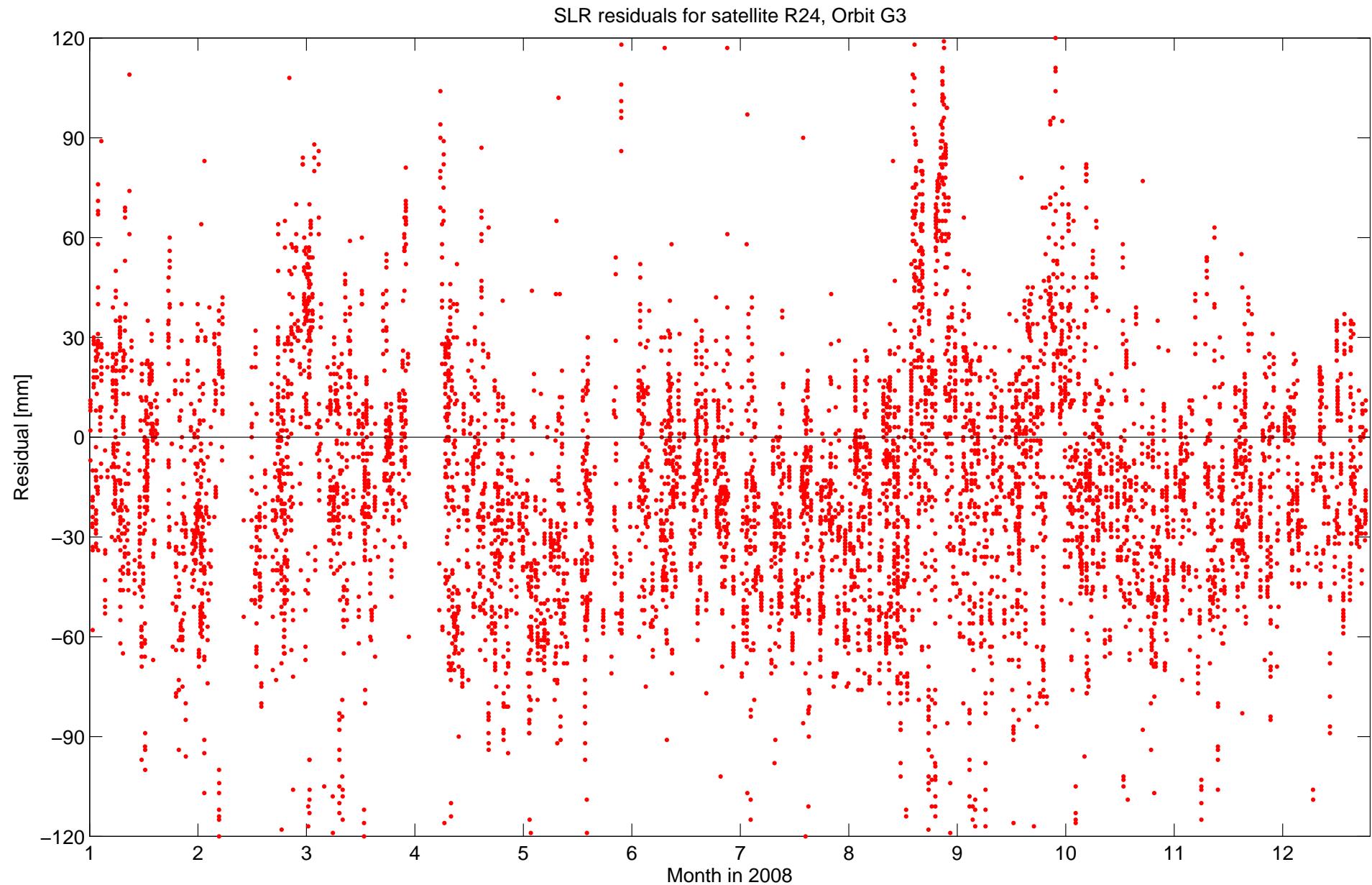
- Switch to new z-offset for GNSS antenna of Glonass satellite R23 within IGS
  - ILRS agreed to track R23 during the transition phase (10 weeks)
- ⇒ Many thanks to all SLR sites for supporting this tracking request!



# SLR residuals



# SLR residuals



# SLR residuals

