Validation and estimation of low-degree gravity field coefficients using LAGEOS

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ABSTRACT

Precise orbit determination is an essential task for analyzing satellite laser ranging (SLR) data. The quality of the satellite orbits directly depends on the background models used for dynamic orbit determination, e.g., on the underlying model of the Earth's gravity field. We investigate the influence of more than ten recent and well known gravity field models on the quality of a combined LAGEOS-1 and LAGEOS-2 orbit determination by analyzing orbital fits. For this purpose we process the SLR data collected by the stations of the International Laser Ranging Service (ILRS) to both LAGEOS satellites in 2008 and show that not only the type and maximum degree of the underlying gravity field model is essential, but also the proper choice of a limited number of empirical orbit parameters that have to be estimated together with all other relevant parameters like station coordinates, Earth orientation parameters, and the satellite's initial conditions on a weekly basis. Based on the experience gained from such validations, the LAGEOS SLR data collected by the ILRS in 2009 are used to estimate weekly corrections to the C_{20} values of the underlying a priori gravity field model, and to accumulate the estimates to monthly corrections.

1   Introduction

The satellite laser ranging (SLR) data to both LAGEOS satellites are processed in a combined analysis based on 7-day arcs using the gravity field models listed in Table 1 (ICGEM, 2011) according to two different solution strategies. For solution (a) one constant empirical acceleration is estimated per 7-day arc for each LAGEOS satellite in the along-track direction in addition to the initial conditions, as well as once-per-revolution (OPR) accelerations in the along-track and cross-track directions. The OPR accelerations in the respective directions are set up as coefficients scaling the cosine and sine of the argument of latitude, i.e., of the angle between the nodal line and the satellite's geocentric position vector as measured from the ascending node. For solution (b) essentially the same parametrization is used, but without estimating the coefficients of the OPR cross-track accelerations. For both solutions the coordinates of the ILRS tracking stations, the Earth orientation parameters, and range biases for selected sites are co-estimated on the same weekly basis.

Gravity field model	Year	Max. degree	Drift	SLR	CHAMP	GRACE	GOCE	Ground data
JGM3	1994	70		X				X
EGM96	1996	360		X				X
EIGEN-GL04C	2006	360	4	X		X		X
EGM2008	2008	2190				X		X
EIGEN51C	2010	359	4	X	X	X		X
ITG-GRACE2010	2010	180				X		
AIUB-CHAMP03S	2010	100			X			
AIUB-GRACE03S	2011	160	30			X		
GO-CONS-2-DIR-R2	2011	240					X	
GOCO02S	2011	250		X	X	X	X	
AIUB - SST - only	2011	120			X		X	

Table 1: Gravity field models and their characteristics

2 Validation of gravity field models

The LAGEOS orbits are sensitive only up to about degree and order 20 of the Earth's gravity field. Orbit solutions only differ slightly when the gravity field coefficients are taken into account up to higher degrees than 14, e.g., on a level of about 0.5 mm for a spherical harmonic expansion up to degree 20. Coefficients above degree 20 do not significantly impact the LAGEOS trajectories.

2.1 Standard solution

Figure 1 shows the root-mean-square (RMS) of the SLR observation residuals obtained from the weekly solutions when using the gravity field models listed in Table 1 and adopting the solution strategy (a). Similar results of good quality are obtained for the majority of the models, apart from EGM96 showing a slightly inferior performance. JGM3 and ITG-GRACE2010 also show a very small degradation with respect to other models. Smallest RMS values are obtained for EGM2008, GO-CONS-2-DIR-R2, AIUB-GRACE03S, EIGEN-51C, and EIGEN-GL04C (7.13, 7.14, 7.15, 7.16, and 7.17 mm, respectively). The RMS of ITG-GRACE2010 may be reduced to 7.18 mm as well, provided that the degree-one coefficients are set to zero. This modified model is labeled as "ITG-GRACE2010 mod" in Fig. 1.
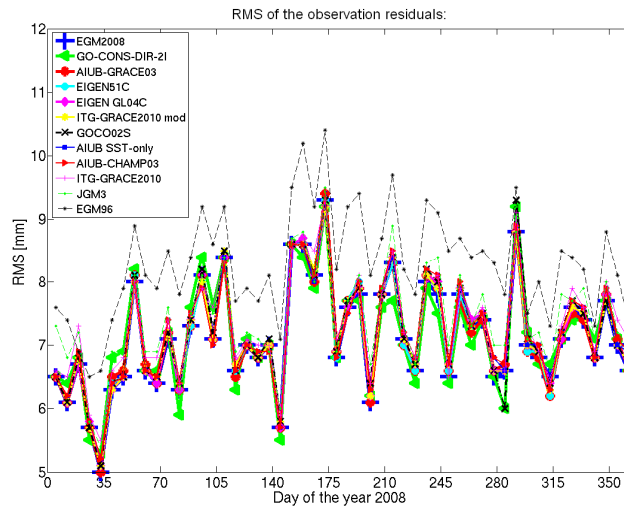

Figure 1: RMS of weekly LAGEOS solutions with the full set of OPR accelerations estimated (solution (a))

2.2 Omission of OPR cross-track accelerations

Figure 2 shows the RMS of the SLR observation residuals obtained from the weekly solutions when using the gravity field models listed in Table 1 and adopting the solution strategy (b). A very pronounced discrimination between the different models is obvious. AIUB-GRACE03S, among the best models when adopting solution strategy (a) (see Fig. 1), is now showing an exceptionally poor performance. Smallest RMS values are obtained for the GPS-only models AIUB-CHAMP03S and AIUB-SST-only (10.51 and 10.52 mm, respectively), where the latter is an extension of the CHAMP-based model with GPS data from GOCE. The best performance of the GRACE-based models is obtained for EIGEN-GL04C with an RMS of 12.56 mm.
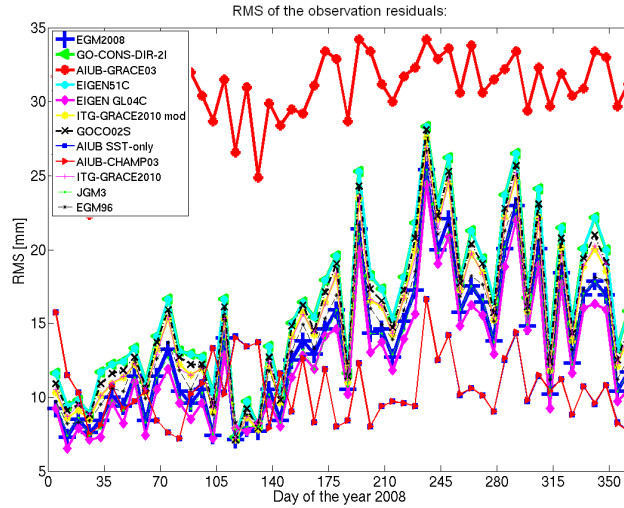
Figure 2: RMS of weekly LAGEOS solutions without OPR cross-track accelerations estimated (solution (b))

2.2.1 Correlation of OPR accelerations with C_{20}

Equation 1 shows the acceleration due to C_{20} in the radial (R), along-track (A), and cross-track (C) directions as a function of the argument of latitude u, the geocentric distance r, the orbital inclination i, and the equatorial radius of the Earth a_e:

$$\begin{pmatrix} R \\ A \\ C \end{pmatrix} = \frac{3}{2} \frac{GMa_e^2 C_{20}}{r^4} \begin{pmatrix} 1 - \frac{3}{2}\sin^2 i + \frac{3}{2}\sin^2 i \cos 2u \\ \sin^2 i \sin 2u \\ \sin 2i \sin u \end{pmatrix}$$

Equation 1: Acceleration due to C_{20}

Since only the cross-track component is governed by a OPR periodicity, Eq. 1 illustrates a full correlation between C_{20} and the sine coefficient of an empirically determined OPR cross-track acceleration per arc. The results of the solution strategy (a) are thus almost insensitive to the quality of the C_{20} coefficient of the used gravity field model. Deficient C_{20} coefficients, such as for AIUB-GRACE03S where C_{20} is derived from GRACE-only, may be perfectly absorbed by the sine coefficient of the empirical OPR cross-track acceleration. Solution strategy (b) is thus well suited to mainly validate the quality of the C_{20} coefficient, whereas solution strategy (a) is well suited to essentially overcome the impact of bad C_{20} coefficients in the analysis. As a consequence, solution strategy (a) cannot be used to estimate C_{20} from SLR data on a weekly basis as it is performed in Sect. 3.

3   Estimation of low-degree gravity field coefficients

Figure 3 shows normalized and unconstrained weekly estimates of C_{20} when using the a priori gravity field model GGM02S and when adopting the solution strategy (b). For comparison with the monthly series from the Center for Space Research (CSR), the weekly estimates are accumulated to monthly solutions as well, and the a priori values of GGM02S are shown as reference. The first result of C_{20} estimates obtained with the Bernese Software (Dach et al., 2007) shows a fair agreement with the series from CSR, including data from Stella, Starlette, and Ajisai in addition.
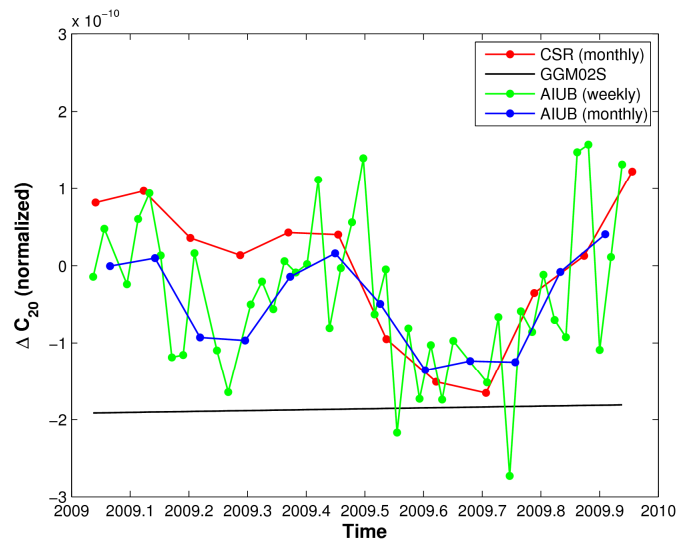
Figure 3: Weekly and monthly estimates of C_{20} w.r.t. $4.84169411 \cdot 10^{-4}$

4 Conclusions

The smallest RMS of fit to the SLR data from LAGEOS-1 and LAGEOS-2 are obtained for the gravity field models EGM2008, GO-CONS-2-DIR-R2, AIUB-GRACE03S, EIGEN-51C, and EIGEN-GL04C when estimating the full set of OPR accelerations. Without estimating OPR cross-track accelerations, the validation results are mainly dominated by the quality of the C_{20} coefficients, e.g., revealing an exceptionally poor quality of C_{20} for AIUB-GRACE03S and best results for the GPS-only models AIUB-CHAMP03S and AIUB-SST-only. First results of C_{20} estimates obtained with the Bernese Software show a fair agreement with the series from CSR when omitting OPR cross-track accelerations. Longer data series will be processed in the near future.

References

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